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# **Example of a Potential Grid Technology application for effective kinetic equation calculations**

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# The Main Idea of Approach

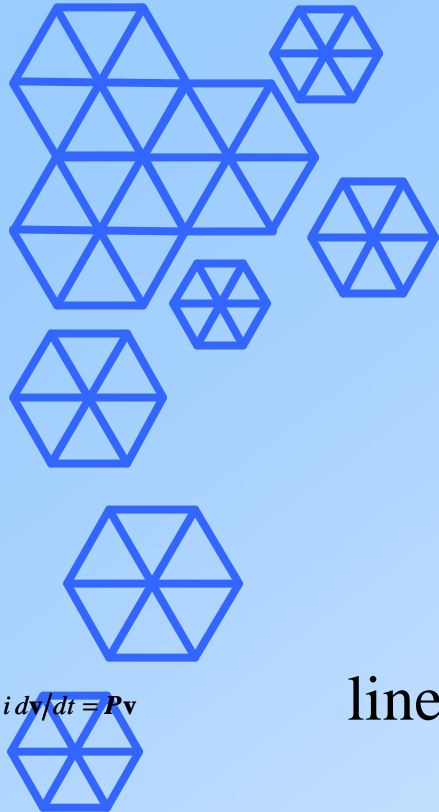
evolution equation of the type

$$du/dt = Pu;$$

linear system ordinary differential equations of the type

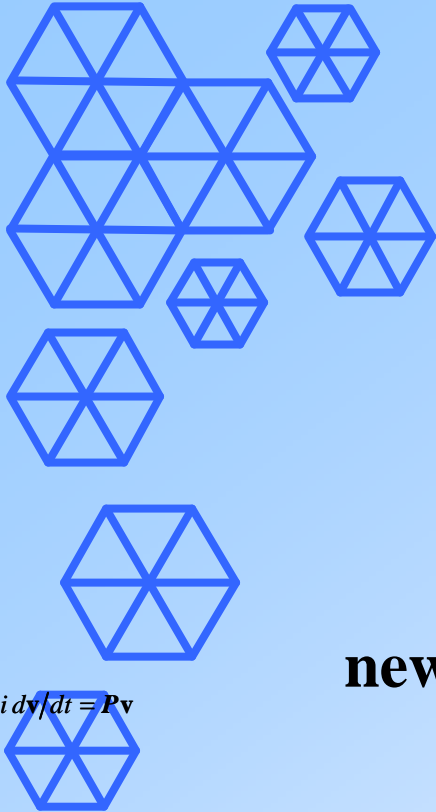
$$dv/dt = Pv;$$

$\mathbf{v}$  - the large vector  $\mathbf{P}$  - symmetric matrix



$i dv/dt = Pv$





## The Equations of Nonequilibrium Kinetics

$$Dc(\mathbf{j}, t)/Dt = I(\mathbf{j} - \mathbf{1}, t) - I(\mathbf{j}, t)$$

$$I(\mathbf{j}, t) = K(\mathbf{j}, \mathbf{j} + \mathbf{1})c(\mathbf{j}, t) - K(\mathbf{j} + \mathbf{1}, \mathbf{j})c(\mathbf{j} + \mathbf{1}, t)$$

**new variables**

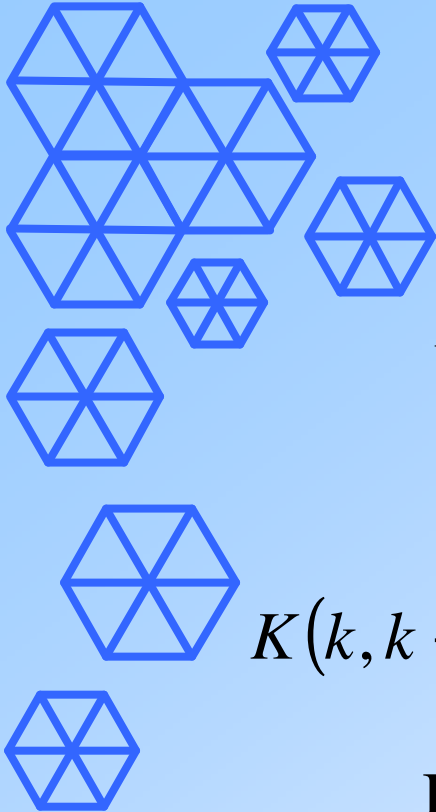
$$f(\mathbf{j}, t) = c(\mathbf{j} + \mathbf{1}, t)/c(\mathbf{j}, t)a(\mathbf{j}, t)$$

$a(\mathbf{j}, t)$  the ratio of to rate constants  $K(\mathbf{j}, \mathbf{j} + \mathbf{1})$   $K(\mathbf{j} + \mathbf{1}, \mathbf{j})$

$$df(\mathbf{j}, t)/dt = \tilde{R}(f(\mathbf{j}, t)) + H(\mathbf{j}, t)f(\mathbf{j}, t) + S(\mathbf{j})f(\mathbf{j}, t)$$

$i dv/dt = Pv$





**Some Particular Cases:  
rotational nonequilibrium flows in jets and nozzles**

$$K(i, j) \rightarrow K^*(i, j) = K(i, j) + n \sum_k K(k, k + 1; i, j) c(k, t)$$

$n$  is the density,

$K(k, k + 1; i, j)$  - rate constant for molecule-molecule collision

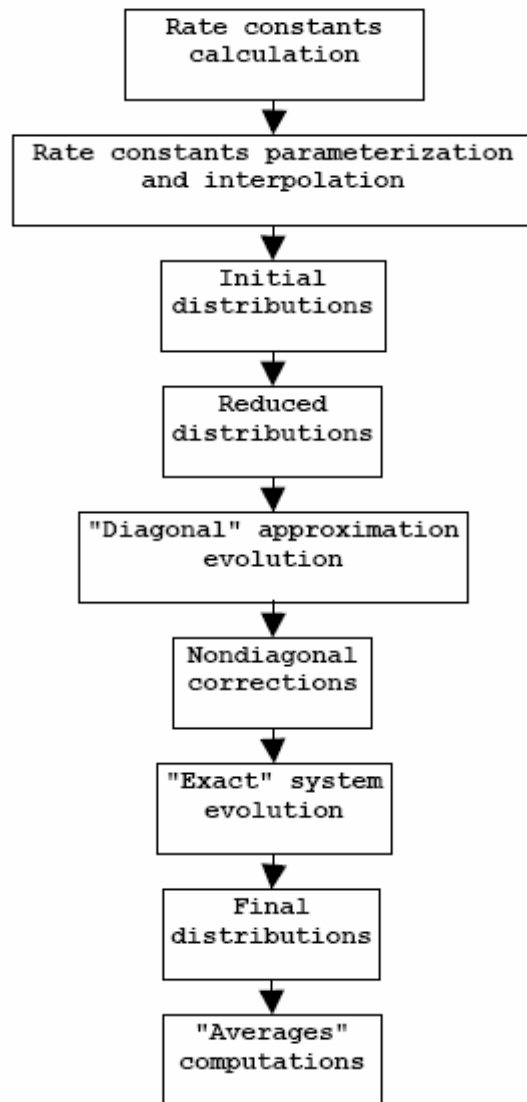
In the zero approximation we have the equation:

$$df(\mathbf{j}, t)/dt = -G(t)\Delta E_{\mathbf{j}} f(\mathbf{j}, t)$$

$$f^{(1)}(\mathbf{j}, t) = \exp\left[-\Delta E_{\mathbf{j}} \int_0^t G(t) dt\right] \int_0^t R(f(\mathbf{j}, t), f(\mathbf{j}, t))_T \exp\left[\Delta E_{\mathbf{j}} \int_0^T G(t_1) dt_1\right] dt,$$



## Stages of the computation



- Rate constants computation,
- Rate constants parametrization,
- Approximate system evolution,
- Corrections for exact system evolution,
- Populations and averages computations

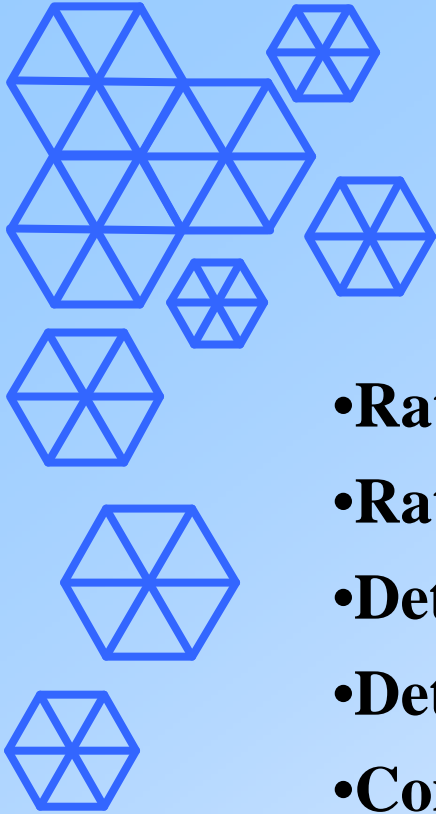


# The basic principles of the Grid for kinetics calculation

- Present computer and data resources as a single virtual environment by developing a web portal on the Grid technology.
- Build an easy-to-use user web interface for providing access to these resources.
- Facilitate the sharing of results of research.
- Organize archiving of input, output, and intermediate data.



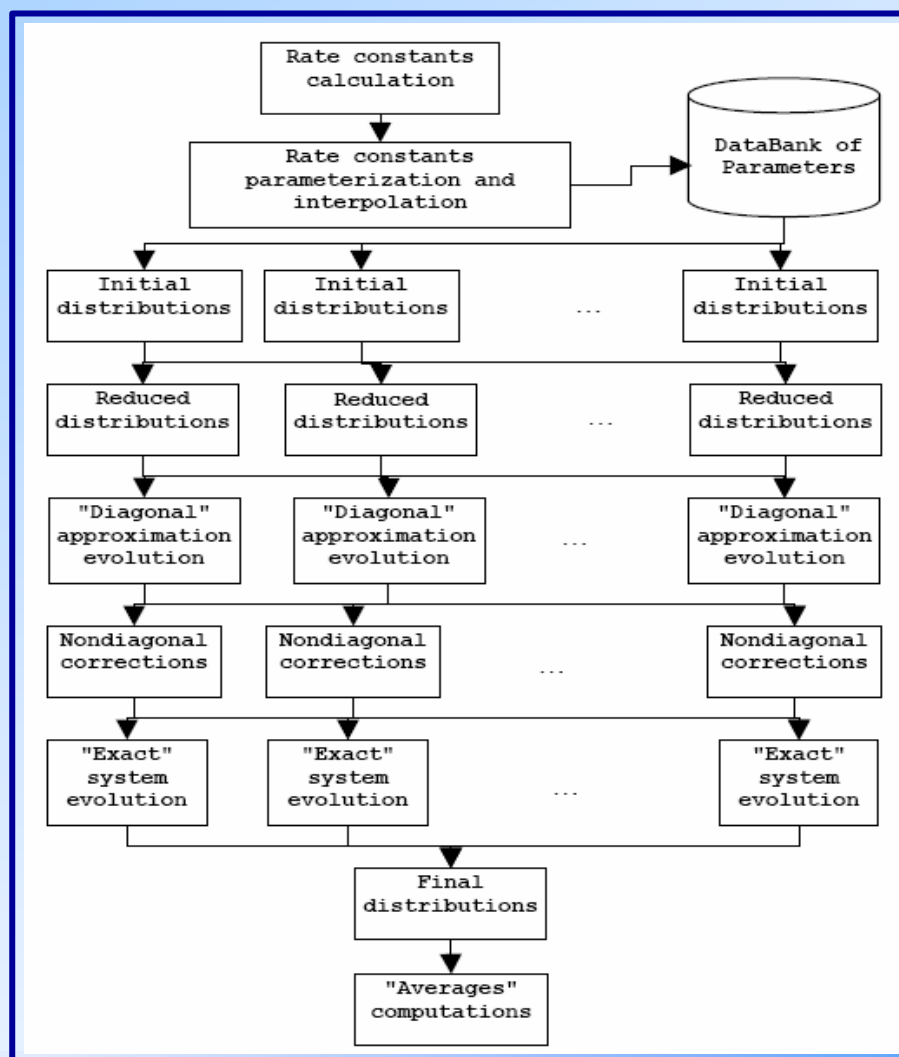
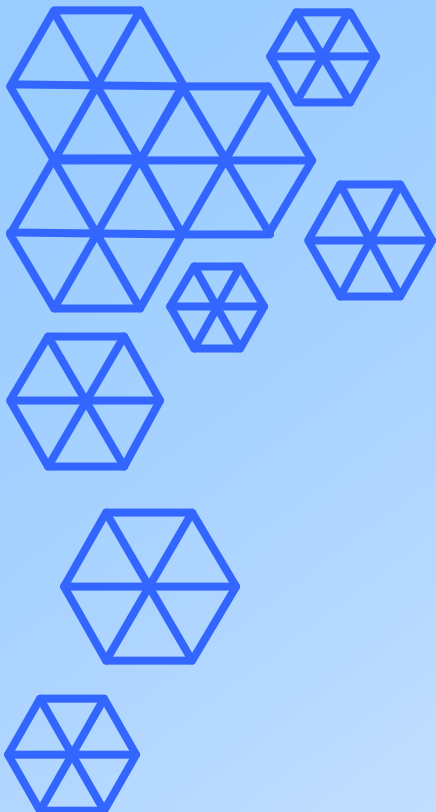
## Using Grid for solution of the reactive scattering problem



- **Rate constants computation,**
- **Rate constants parametrization,**
- **Determination of initial values of reduced populations,**
- **Determination of how far from equilibrium is the state,**
- **Computation of diagonal or nearequilibrium approximation,**
- **Computation of exact solution corrections,**
- **Determination of final distributions,**
- **Computations of averages,**
- **Visualization of the results.**

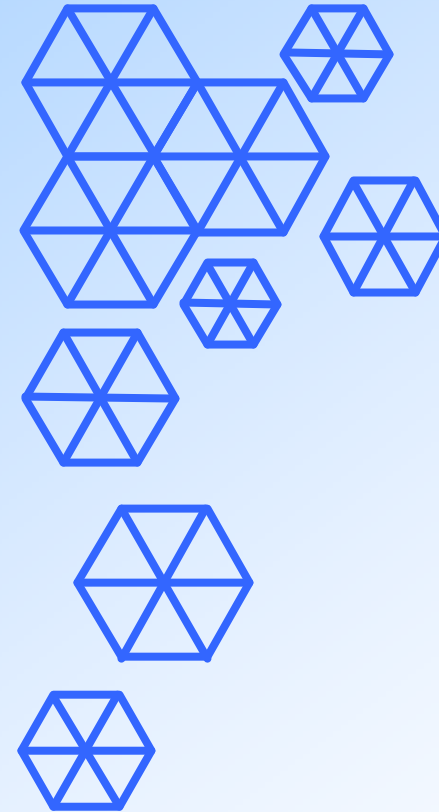
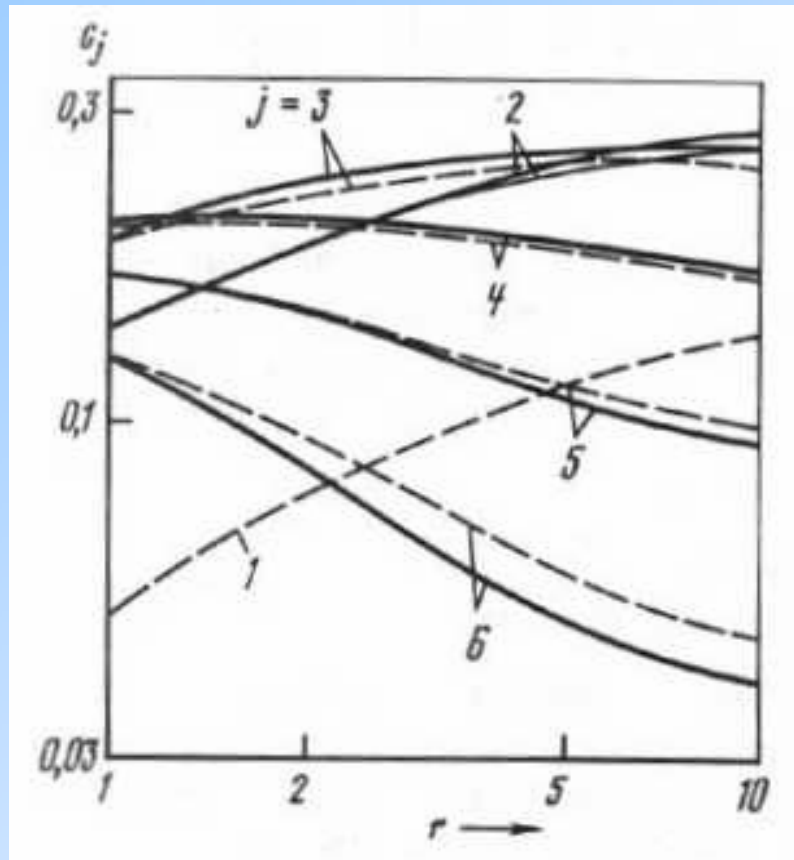


# The parallel scheme of computing process.





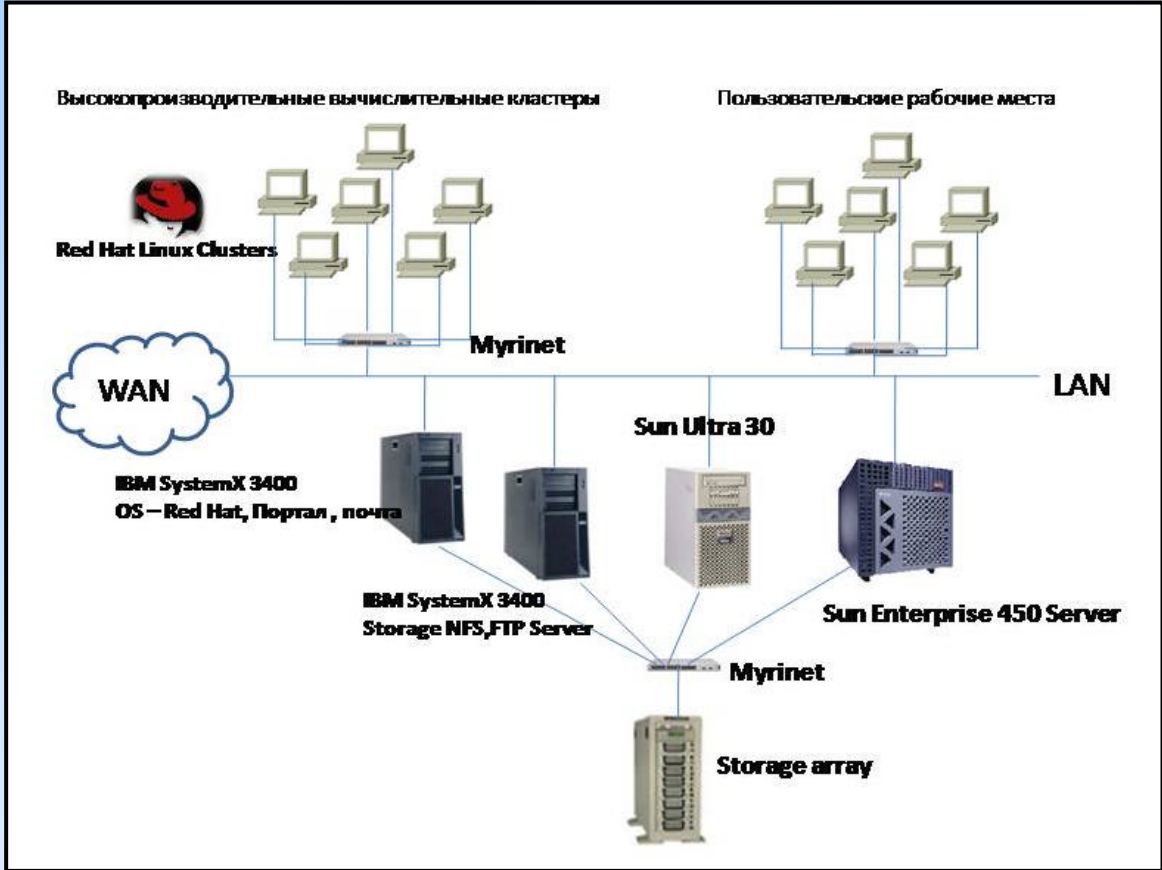
# Important Example



The difference between exact (solid lines) and diagonal approximation (dashed lines) populations for He-HF mixture nozzle flow



# TESTBED



# Conclusions

**The use of some physical considerations makes it possible:**

- to derive some new algorithms for solution of the evolution equations for physical variables like distribution function
- to reduce the needed computer time orders of magnitude
- go to substantially larger number of processor
- work out approximate methods, which can be used for mass computations in technical applications.
- essentially reduce computational time in comparison with the parallel approach

